$f:(R, \dot{R}) \to (\tau, \dot{\tau})$. Using f in conjunction with the new surgery groups of Cappell-Shaneson, a splitting obstruction can be defined along any singular Z_q -manifold $g:(V, \delta V) \to M$ as in [6]. By the universal coefficient theorem for $K_{F/TOP}^*$, these represent an element $\gamma(M, N) \in K_{F/TOP}^*(M, G_{\bullet+1})$.

 β . For large r, $f \times 1_{D'}$: $(R, R) \times (D^r, \partial D^r) \to (\tau, \tau) \times (D^r, \partial D^r)$ represents an element $\beta(M, N) \in K^0_{F/PL}(M)$.

REMARK 1. There is a classifying space BSPL² (2) for codimension 2 PL thickenings of PL manifolds. There are universal characteristic classes

$$\theta \in H^2(BSPL^{\sim}(2), G_3),$$

 $\beta \in K^0_{F/PL}(BSPL^{\sim}(2)),$
 $\gamma \in K^0_{F/TOP}(BSPL^{\sim}(2), G_{*+1}).$

Modulo low-dimensional complications (over the 4 skeleton of $BSPL^{\infty}(2)$) there is a homotopy equivalence

$$BSPL^{\sim}(2) \xrightarrow{f \times \gamma} BSO(2) \times (\overline{F/TOP} \otimes G_{*+1}).$$

REMARK 2. The classes θ , β , γ are related as follows. The geometric stabilization of θ is determined by the restriction of γ to the 2-skeleton of M. The stabilization of β is a direct summand of γ .

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APPLICATIONS OF THE TRANSFER TO STABLE HOMOTOPY THEORY

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In this note we outline the construction, properties and several applications of a transfer morphism for the generalized cohomology of finite coverings. Our principal application consists of a proof of a conjecture of M. E. Mahowald [9] and G. W. Whitehead [14]. Let $\lambda: \Sigma^n RP^{n-1} \to S^n$ be the adjoint of $RP^{n-1} \xrightarrow{i_n} O_n \xrightarrow{j_n} \Omega^n S^n$ where i_n represents a line L through the origin in R^n as the reflection in the hyperplane perpendicular to L and j_n represents an element of O_n as a map $(R^n \cup \infty, \infty) \to (R^n \cup \infty, \infty)$. Then, for 0 < i < n-1,

$$\lambda_{n+i}: \pi_{n+i}(\Sigma^n R P^{n-1}) \to \pi_{n+i}(S^n)$$

is an epimorphism of 2-primary components (see §3).

The existence of the transfer seems to be well known [13], but we know of no published account. In §1 we outline such a construction. The essential connection between the transfer and stable homotopy theory is provided by a stable map which yields the transfer as an induced homomorphism (Proposition 1.7). As an immediate consequence, the transfer commutes with stable cohomology operations. This generalizes the same result for ordinary cohomology of groups proved by Evens [7]; similarly it gives an alternate proof of Quillen's result [12] that the localized Adams operations $\psi^p[p^{-1}]$ commute with the transfer in K-theory. As a final application we given a stable decomposition of $(\Omega^{\infty}S^{\infty})_0$. Details will appear elsewhere,

We would like to thank M. G. Barratt and M. E. Mahowald for many helpful conversations. Further thanks are due J. F. Adams for his critical comments on an earlier version of this work. In particular, he pointed out that our original argument could be modified so that the epimorphism (0.1) derives from a geometric splitting (see Theorem 3.1). A more detailed analysis of this point will appear in a forthcoming article by Adams. We have recently learned that F. W. Roush has also studied the transfer.

1. The transfer for generalized cohomology. Let $\pi: E \to B$ be a finite covering of degree N (for the purposes of this note we assume E

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connected). Let $\pi_1(E) = H$, $\pi_1(B) = G$; then we may replace $\pi: E \to B$ by the homeomorphic covering $p: X/H \to X/G$ where X is the universal covering space of B (acted upon freely on the right by G) and p is the projection. Let $G/H = \{\tau_1 H, \tau_2 H, \ldots, \tau_N H\}$ be the left cosets of H in G; then G acts on the left of G/H as a group of permutations, i.e., we have a representation $\rho: G \to \mathscr{S}_N$ ($\mathscr{S}_N = \text{symmetric group on } \{1, \ldots, N\}$) defined by $g\tau_i = \tau_{\rho(g)(i)}h_i$ for $g \in G$ and uniquely determined $\rho(g) \in \mathscr{S}_N$ and $h_i \in H$.

Let WG be a contractible CW complex on which G acts freely on the left and similarly for $W\mathcal{S}_N$. Define

$$\Phi: X \underset{G}{\times} WG \to (X/H)^N \underset{\mathscr{S}_N}{\times} W\mathscr{S}_N$$

by $\Phi(x,\omega)=(\overline{x\tau_1},\ldots,\overline{x\tau_N},\rho_*(\omega))$ where G acts on the left of X by $g\cdot x=xg^{-1}$ and \mathcal{S}_N acts on the left of $(X/H)^N$ by permuting coordinates, i.e. $\sigma(x_1,\ldots,x_N)=(x_{\sigma^{-1}(1)},\ldots,x_{\sigma^{-1}(N)})$. The element $\overline{x\tau_i}$ is the class of $\overline{x\tau_i}$ in X/H and $\rho:WG\to W\mathcal{S}_N$ is the induced map.

Lemma 1.1. Φ is well defined and its homotopy class $[\Phi]$ is independent of the choice of coset representatives $\{\tau_i\}$.

Because of the evident homotopy equivalence $X/G \simeq X \times_G WG$ we shall often consider Φ as a map $\Phi: X/G \to (X/H)^N \times_{\mathscr{S}_N} W\mathscr{S}_N$.

REMARK 1.2. Evens [8] has defined a group monomorphism $G \to \mathscr{S}_N \cap H$. It can be shown that the induced map $BG \to B(\mathscr{S}_N \cap H) = (BH)^N \times_{\mathscr{S}_N} W\mathscr{S}_N$ agrees up to homotopy with Φ for the covering WG/H - WG/G. $(\mathscr{S}_N \cap H)$ is the wreath product [8].)

Let $(\cdot)^+$ denote the addition of a disjoint point as base point.

DEFINITION. 1.3. The pretransfer $T: X/G \to ((X/H)^+)^N \times_{\mathscr{S}_N} W\mathscr{S}_N$ for the N-fold covering $p: X/H \to X/G$ is the composite

$$X/G \stackrel{\Phi}{\to} (X/H)^N \underset{\mathscr{S}_N}{\times} W\mathscr{S}_N \to ((X/H)^+)^N \underset{\mathscr{S}_N}{\times} W\mathscr{S}_N,$$

where the second map is induced by the inclusion $(X/H) \rightarrow (X/H)^+$.

We now define the transfer morphism. Suppose $\mathscr Y$ is an Ω -spectrum. (All Ω -spectra and morphisms of such are assumed strict, i.e. $\mathscr Y_i = \Omega \mathscr Y_{i+1}$, etc. May [10] shows that these spectra are adequate.) Recall that there are Dyer-Lashof maps [4]

$$\theta_q^N(\mathcal{Y}) \,=\, \theta_q^N \,; \mathcal{Y}_q^N \underset{\mathcal{S}_N}{\times} \, W \mathcal{S}_N \to \mathcal{Y}_q$$

defined using the iterated loop space structure of \mathcal{Y}_a .

DEFINITION 1.4. The (\mathscr{Y} -cohomology) transfer morphism, for the N-fold covering $p: X/H \to X/G$, $p': H^q(X/H; \mathscr{Y}) \to H^q(X/G; \mathscr{Y})$ is defined by $p'(\alpha) = [\theta_q^N \circ (a^N \times_{\mathscr{S}_N} 1) \circ T]$,

 $(X/G) \xrightarrow{T} ((X/H)^+)^N \underset{\mathscr{S}_N}{\times} W\mathscr{S}_N \xrightarrow{a_N \times \mathscr{S}_N} (\mathscr{Y}_q)^N \underset{\mathscr{S}}{\times} W\mathscr{S}_N \xrightarrow{\theta_q^N} \mathscr{Y}_q$

where $a:(X/H)^+ \to \mathcal{Y}_q$ represents $\alpha \in H^q(X/H; \mathcal{Y})$.

PROPOSITION 1.5. p^t is well defined and natural with respect to morphisms of covering maps and morphisms of Ω -spectra. Moreover, p^t commutes with compositions of coverings.

1.6. Set $Q((X/H)^+) = \bigcup_n \Omega^n \Sigma^n((X/H)^+)$. Let $f: (X/G)^+ \to Q((X/H)^+)$ be the pointed extension to $(X/G)^+$ of $\theta_q^N \circ (i^N \times_{\mathscr{S}_N} 1) \circ T$ (see Definition 1.4), where $i: (X/H)^+ \to Q((X/H)^+)$ is the inclusion, i.e. $[f] = p!([i]) \in H^0(X/G; \mathscr{Y})$ for the Ω -spectrum \mathscr{Y} with $\mathscr{Y}_k = Q(\Sigma^k((X/H)^+))$. (\mathscr{Y} is the Ω -spectrum associated to the suspension spectrum of $(X/H)^+$.) If X is I-dimensional, f is homotopic to a map $\hat{f}: (X/G)^+ \to \Omega^{l+1} \Sigma^{l+1}((X/H)^+) \subset Q((X/H)^+)$. Thus $(\text{adj } \hat{f}): \Sigma^{l+1}((X/G)^+) \to \Sigma^{l+1}((X/H)^+)$. With this notation we state

PROPOSITION 1.7. If X/H has finite dimension l and $\mathscr E$ is an Ω -spectrum, then

$$H^*(X/H;\mathscr{E}) \xrightarrow{p!} H^*(X/G;\mathscr{E})$$

$$\approx \uparrow \sigma \qquad \qquad \approx \uparrow \sigma$$

$$H^{*+l+1}(\Sigma^{l+1}((X/H)^+);\mathscr{E}) \xrightarrow{\text{(adj } \hat{f})^*} H^{*+l+1}(\Sigma^{l+1}((X/G)^+);\mathscr{E})$$

commutes, where σ denotes the suspension isomorphism.

COROLLARY 1.8. p! is a homomorphism and commutes with stable cohomology operations for finite complexes.

2. Agreement with other definitions of the transfer. Let $t^*: H^*(X/H; A) \to H^*(X/G; A)$ denote the ordinary cohomology transfer [6] for the N-fold covering $p: X/H \to X/G$ where A is an abelian group.

PROPOSITION 2.1. Let $\mathcal{K}(A)$ denote the Eilenberg-Mac Lane spectrum. Then

$$t^* = p^!: H^*(X/H; \mathcal{K}(A)) \to H^*(X/G; \mathcal{K}(A)),$$

i.e. the transfer p' agrees with the classical transfer for ordinary cohomology theory.

REMARK 2.2. Consider the situation of Proposition 1.7. It follows from the universal coefficient theorem that the induced ordinary homology homomorphism (adj \hat{f})_{*} with Z_p coefficients (p a prime) is equivalent to the classical ordinary homology transfer. This fact can be proved directly and holds also for the case of integer coefficients.

REMARK 2.3. In the situation of Proposition 1.7, consider the map

EMARK 2.3. In the situation of Tropostal (adj
$$\hat{f}$$
): $\Sigma^{l+1}((X/G)^+) = \Sigma^{l+1}(X/G) \vee S^{l+1} \to \Sigma^{l+1}(X/H) \vee S^{l+1} = \Sigma^{l+1}((X/H)^+).$

Since $\Sigma^{l+1}(X/H)$ is (l+1)-connected, one may pinch to a point the two (l+1)-spheres and obtain a map $\Sigma^{l+1}(X/G) \to \Sigma^{l+1}(X/H)$ whose induced homology homomorphism is equivalent to the transfer on reduced homology groups.

To obtain similar results for K-theory, one observes that Atiyah's definition [1] of the transfer bundle $\rho_*(E): X/G \to BU_{Nk}$ of a bundle $E: X/H \to BU_{\nu}$ is given by

$$E: X/H \to BU_k \text{ is given by}$$

$$X/G \xrightarrow{E} (X/H)^N \underset{\mathscr{S}_N}{\times} W\mathscr{S}_N \xrightarrow{E^N \times \mathscr{S}_{N^1}} (BU_k)^N \underset{\mathscr{S}_N}{\times} W\mathscr{S}_N = B(\mathscr{S}_N \cap U_k) \to BU_{Nk}$$

$$Then$$

Proposition 2.4. Let ${\mathcal K}$ denote either the BU or BO spectrum. Then

$$\rho_* = p^! : H^*(X/H; \mathcal{K}) \to H^*(X/G; \mathcal{K}),$$

i.e. the transfer p' agrees with Atiyah's transfer for K-theory.

The proof relies on the homotopy commutative diagram

$$(BU_{k})^{N} \times W\mathcal{S}_{N} = B(\mathcal{S}_{N} \cap U_{k}) \to BU_{kN}$$

$$\downarrow \qquad \qquad \downarrow$$

$$(BU)^{N} \times W\mathcal{S}_{N} \xrightarrow{\theta^{N}(BU)} BU$$

of Boardman (unpublished). Similarly for U replaced by O.

component of a map $S^n \to S^n$ of degree m, and let $\gamma_m : B\mathscr{S}_m \to (QS^0)_0$ be the composite map

the composite map
$$B\mathcal{S}_m = [1]^m \underset{\mathcal{S}_m}{\times} W\mathcal{S}_m \to ((QS^0)_1)^m \underset{\mathcal{S}_m}{\times} W\mathcal{S}_m \xrightarrow{\theta^m} (QS^0)_m \xrightarrow{*[-m]} (QS^0)_0$$

where θ^n is the Dyer-Lashof map and * is the loop product for QS We shall equate $B\mathcal{S}_2 = RP^{\infty}$ and write $\gamma = \gamma_2 : RP^{\infty} \to (QS^0)_0$, γ has a canonical extension $\bar{\gamma}: Q(RP^{\infty}) \to (QS^0)_0$ (see below). Similarly for any map $\phi: RP^{\infty} \to (QS^0)_0$.

THEOREM 3.1. Let $\phi: RP^{\infty} \to (QS^0)_0$ be a map such that $\phi_*(e_1) = \gamma_*(e_1)$ where e_1 is the generator of $H_1(RP^{\infty}; Z_2)$. Then there exists a map $\psi: (QS^0)_0 \to Q(RP^\infty)$ such that $\overline{\phi} \circ \psi$ is a mod 2 equivalence, i.e. $\overline{\phi}$ splits mod 2.

damental group will do. In particular the map λ of the introduction is inverse limit argument (using finiteness of all homotopy groups in sight) REMARK 3.2. Any $\phi: RP^{\infty} \to (QS^{0})_{0}$ which is nontrivial on the fun-

such a ϕ . It is an immediate consequence of Theorem 3.1 that the homomorphism (0.1) is surjective.

Before sketching a proof of Theorem 3.1, we recall that there is a natural transformation $h: QQ(\cdot) \to Q(\cdot)$ such that, if Y is an infinite loop space with retraction map $r: QY \to Y$ [10, p. 451], then $r \circ Q(r) = r \circ h_Y$. (If $\phi: X \to Y$, $\phi = r \circ Q(\phi): QX \to Y$ is the canonical extension mentioned above.) We fix the following notation: $\hat{Q}_m(\cdot) = (\cdot)^m \times_{\mathscr{G}_m} W\mathscr{S}_m$ and $\mathscr{G}(2^k,2)$ is a 2-Sylow subgroup $\mathscr{G}_2 \cap \mathscr{G}_2$ (k-fold wreath product) of \mathcal{G}_{2^k} . We have $B\mathcal{S}(2^k,2) = \hat{Q}_2 \dots Q_2 B\mathcal{S}_2$ $(k-1\hat{Q}_2$'s). Recall that the index $m = \lceil \mathcal{S}(2^k, 2) : \mathcal{S}_{2^k} \rceil$ is odd.

SKETCH OF PROOF OF THEOREM 3.1. Consider the following two composite maps:

$$\Sigma^{\infty}B\mathscr{S}_{2^{k}} \xrightarrow{f_{1}} \Sigma^{\infty}B\mathscr{S}(2^{k}, 2) \xrightarrow{f_{2}} \Sigma^{\infty}B\mathscr{S}_{2^{k}} \xrightarrow{f_{3}} \Sigma^{\infty}(QS^{0})_{0},$$

(3.4)
$$\Sigma^{\infty}B\mathscr{S}_{2^{k}} \xrightarrow{f_{1}} \Sigma^{\infty}B\mathscr{S}(2^{k}, 2) = \Sigma^{\infty}\hat{Q}_{2} \cdots \hat{Q}_{2}B\mathscr{S}_{2} \xrightarrow{g_{2}} \Sigma^{\infty}\hat{Q}_{2^{k-1}}B\mathscr{S}_{2}$$
$$\xrightarrow{g_{3}} \Sigma^{\infty}QB\mathscr{S}_{2} \xrightarrow{g_{4}} \Sigma^{\infty}(QS^{0})_{0}$$

and set $F = f_3 f_2 f_1$, $G_{\phi} = g_4 g_3 g_2 f_1$.

 Σ^{∞} denotes the suspension spectrum functor. f_1 is the map of Remark 2.3 associated to the covering $B\mathcal{S}(2^k,2) \to B\mathcal{S}_{2^k}$; f_2 is induced by the inclusion $\mathscr{S}(2^k,2)\subset S_{2^k}; f_3=\Sigma^{\infty}\gamma_{2^k}; g_2$ is induced by the wreath product; g_3 a Dyer-Lashof map for $QB\mathscr{S}_2$; and g_4 is $\Sigma^{\infty}(\overline{\phi})$. With the exception of f_1 , each of these is Σ^{∞} of a map.

$$(f_2f_1)_*: H_*(\Sigma^\infty B\mathscr{S}_{2^k}; Z_2) \to H_*(\Sigma^\infty B\mathscr{S}_{2^k}; Z_2)$$

3. Applications. (i) Let [m] denote the base point of $(QS^0)_m$, the path is the identity since the ordinary homology transfer followed by inclusion is multiplication by the index, which in this case is odd. Since γ_{2^k} is a mod 2 homology isomorphism in dimensions $\leq 2^{k-1}$ [3], [11], F_* is a mod 2 homology isomorphism in dimensions $\leq 2^{k-1}$. An augmentation type filtration argument comparing F_* to $G_{\gamma *}$ shows that $G_{\gamma *}$ is also a mod 2 isomorphism in dimensions $\leq 2^{k-1}$. Then a length type filtration argument comparing $G_{\gamma*}$ to $G_{\phi*}$ shows that $G_{\phi*}$ is a mod 2 isomorphism in dimensions $\leq 2^{k-1}$.

Apply Ω^{∞} , restrict to 2-primary factors and obtain a commutative diagram

$$2(QB\mathcal{S}_{2^{k}})^{\frac{\Omega^{\infty}g_{3}g_{2}f_{1}}{\longrightarrow}}QQRP^{\infty} \xrightarrow{Q\overline{\phi}} 2(Q(QS^{0})_{0})$$

$$\downarrow h_{1} \qquad \qquad \downarrow h_{2}$$

$$QRP^{\infty} \xrightarrow{\overline{\phi}} 2((QS^{0})_{0}).$$

 $(Q\bar{\phi})\circ(\Omega^{\infty}g_3g_2f_1)$ is a mod 2 equivalence in dimensions $\leq 2^{k-1}$. An

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provides a map $k: {}_{2}(Q(QS^{0})) \to QQRP^{\infty}$ such that $(Q\overline{\phi}) \circ k$ is homotopic to the identity map. Let $i: {}_{2}(QS^{0})_{0} \to {}_{2}Q(QS^{0})_{0}$ be the canonical section of h_{2} . Then $\psi = h_{1} \circ k \circ i$ satisfies Theorem 3.1 on 2-primary factors. Theorem 3.1 now follows.

REMARK 3.5. An analogous result holds for odd primes using $p(B\mathcal{S}_p)$ in place of $B\mathcal{S}_2$. Let $\phi: p(B\mathcal{S}_p) \to (QS^0)_0$ be any map such that ϕ_* is nontrivial on $H_{2p-3}(\ ; Z_p)$. Then $\bar{\phi}: Q(p(B\mathcal{S}_p)) \to (QS^0)_0$ splits mod p.

(ii) In [5], Dold gives an elegant proof of Nakaoka's decomposition of the homology groups of $B\mathcal{S}_n$. Using Proposition 1.7, one can geometrically mimic Dold's proof obtaining

PROPOSITION 3.6. For $2 \le n \le \infty$, there is an equivalence of spectra

$$\Sigma^{\infty}(B\mathscr{S}_n) \to \bigvee_{k=2}^n \Sigma^{\infty}(B\mathscr{S}_k/B\mathscr{S}_{k-1}).$$

PROPOSITION 3.7. For $2 \le n \le \infty$, there is a homotopy equivalence

$$Q(B\mathscr{S}_n) \to \prod_{k=2}^n Q(B\mathscr{S}_k/B\mathscr{S}_{k-1}).$$

We observe that the homology equivalence $B\mathscr{S}_{\infty} \to (QS^0)_0$ [3] implies the corresponding decompositions for $\Sigma^{\infty}(QS^0)_0$ and $Q(QS^0)_0$. (Compare [2].)

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